

# Stabilization of a protein conferred by an increase in folded state entropy

Shlomi Dagan<sup>a</sup>, Tzachi Hagai<sup>b,1</sup>, Yulian Gavrillov<sup>b</sup>, Ruti Kapon<sup>a</sup>, Yaakov Levy<sup>b,2</sup>, and Ziv Reich<sup>a,2</sup>

Departments of <sup>a</sup>Biological Chemistry and <sup>b</sup>Structural Biology, Weizmann Institute of Science, Rehovot 76100, Israel

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**Entropic stabilization of native protein structures typically relies on strategies that serve to decrease the entropy of the unfolded state. Here we report, using a combination of experimental and computational approaches, on enhanced thermodynamic stability conferred by an increase in the configurational entropy of the folded state. The enhanced stability is observed upon modifications of a loop region in the enzyme acylphosphatase and is achieved despite significant enthalpy losses. The modifications that lead to increased stability, as well as those that result in destabilization, however, strongly compromise enzymatic activity, rationalizing the preservation of the native loop structure even though it does not provide the protein with maximal stability or kinetic foldability.**

protein folding | loop closure entropy | molecular dynamics

**R**educing the difference in entropy between the unfolded and folded states can increase the thermodynamic stability of a protein. This is commonly accomplished by strategies that act to restrict the conformational space available for the unfolded state (e.g., decreasing loop length, macromolecular crowding, and backbone cyclization) (1). In principle, changes that increase the entropy of the folded state can also lead to its stabilization provided that they exceed the loss of enthalpic contributions, if stabilizing interactions are perturbed by the modifications.

The current work originally aimed at studying the effects exerted by changes in the length of a loop region on protein stability and folding. As a model, we chose a loop in human muscle acylphosphatase (hmAcP), a small (~100 aa) enzyme that catalyzes the hydrolysis of the carboxyl-phosphate bond in various acylphosphate compounds and presents an open  $\alpha/\beta$ -sandwich structure (ref. 2, and see, e.g., refs. 3–5). The folding stability and dynamics of hmAcP have been studied extensively and are well characterized (ref. 6–10 and references therein). Excluding a minor *cis-trans* prolyl isomerization phase, it folds in a two-step process, albeit very slowly (due to abundance of long-range interactions; ref. 9), through a relatively compact, native-like transition state. The loop we chose for the modifications (hereafter referred to as L4) connects between the second helix and the fourth  $\beta$ -strand of the protein (Fig. 1) and possesses multiple internal and external contacts (refs. 3 and 4 and our own contact analysis). The latter contacts are formed predominantly with residues located in the first loop of the protein (L1), which runs along L4 and is involved in the binding of the phosphate group of the substrate (4, 11–15).

Characterizing the properties of hmAcP mutants carrying deletions or insertions in L4 we found that the thermodynamic stability of mutants in which the loop was shortened is increased to an extent significantly larger than that predicted by polymer models for loop closure entropy. The increased stability is predominantly due to a decrease in the unfolding rate and is attained despite the fact that shortening of the loop is accompanied by considerable losses in enthalpy. Given the above, we postulated that the surplus stabilization arises from an increased conformational entropy of the folded state ensemble. We provide evidence that supports this hypothesis and show that the enhanced dynamics are accompanied by only relatively small rearrangements in secondary and tertiary structure. The thermodynamically

stabilized mutants, as well as the destabilized variants carrying elongated loops, are all deficient in enzymatic activity, suggesting that the native structure of the loop has evolved primarily for function.

## Results and Discussion

The WT and mutant proteins used in the study were derived from the C21S variant of hmAcP, which was used to avoid complications associated with free cysteine residues (7). This mutant is referred to in the manuscript as WT hmAcP. The structure of hmAcP has not been determined. However, the horse ortholog, for which a solution structure is available (3), differs from hmAcP in only five amino acids, all of which are located outside L4. We used this structure to generate models of WT hmAcP, as well as of the various loop-length variants used in the experiments and in the molecular dynamics (MD) simulations (see also refs. 10, 16, and 17).

Table 1 lists the L4 deletion and insertion mutants that were constructed. The site chosen for the modifications encompasses the two adjacent serine residues at positions 72 and 73, which are located in a  $\beta$ -bulge at the tip of L4 that points toward the solvent. This location was considered favorable in terms of end effects and potential interactions between the inserts and the protein. The deletion series consists of three mutants in which two to six residues were removed in a pairwise fashion, starting with the two serine residues and progressing symmetrically outward. These mutants are designated  $\Delta 2$ ,  $\Delta 4$ , and  $\Delta 6$ . The deletions made in the  $\Delta 4$  and  $\Delta 6$  mutants include Pro71, the substitution of which to alanine was previously shown to result in destabilization of the protein (9). However, as discussed below, all of the deletion mutants we constructed are more stable than the WT. The elongated loop mutants, designated  $\nabla 2$ – $\nabla 12$ , contain stretches of 2, 4, 6, 8, and 12 glycine residues (marked in boldface in Table 1), which were inserted between the two serine residues. Far-UV circular dichroic (Fig. S14 and Table S1) and fluorescence emission spectra (Fig. S1C) recorded for the mutants revealed only small variations from the WT protein, indicating that the modifications in L4 do not lead to major alterations in secondary or tertiary structure. All mutants have a relative contact order similar to that of the WT (about 20%) and kinetically folded and unfolded in a two-state manner (excluding the proline isomerization phase).

Thermodynamic parameters derived for the proteins from equilibrium urea denaturation and differential scanning calorimetry (DSC) are listed in Table S2 and drawn in Fig. 2. Going from the mutant carrying the longest loop,  $\nabla 12$ , one sees only a very

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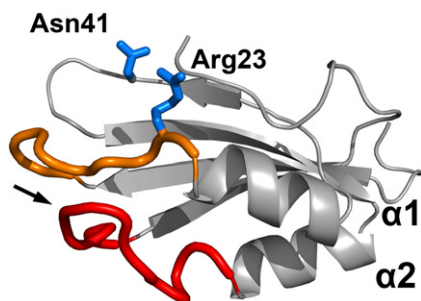
The authors declare no conflict of interest.

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<sup>1</sup>Present address: Department of Microbiology and Immunology, University of California, San Francisco School of Medicine, San Francisco, CA 94158.

<sup>2</sup>To whom correspondence may be addressed. E-mail: koby.levy@weizmann.ac.il or ziv.reich@weizmann.ac.il.

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**Fig. 1.** Model of hmAcP, constructed based on the solution structure of horse muscle AcP (Protein Data Bank ID code 1AP5). L4 (residues 64–77) and the catalytic loop (L1, residues 15–24) are shown in red and orange, respectively. The conserved Arg23 and Asn41 residues, which respectively function in the binding of the substrate's phosphate group and the catalytic water molecule, are shown in stick representation. The arrow marks the location of Ser72 and Ser73, which served as the site for modifications in L4.

small change in stability (0.5 kJ/mol) up to the  $\nabla 6$  insertion mutant (Fig. 2A). As the length of the loop decreases further, the resistance of the proteins to chemical denaturation increases significantly more rapidly, leading eventually to an additional stabilization of  $\sim 18$  kJ/mol. The dependence on loop length of the thermal stability of the proteins exhibits a pattern that is very similar to the one derived from the chemical denaturation experiments (Fig. 2B), finally bringing the heat resistance of the mutant carrying the shortest loop ( $\Delta 6$ ) to the range of thermophilic proteins.

Fig. 2C shows the dependence of the calorimetric unfolding enthalpy,  $\Delta H_m$ , on loop length. Moving from the WT to  $\Delta 6$ ,  $\Delta H_m$  decreases rapidly, eventually dropping by more than 50 kJ/mol. This decrease is most likely due to disruption of interactions involving residues in L4 upon the truncations, effected directly, by the removal of residues engaged in interactions, or indirectly, as a result of alterations in loop geometry. Elongation of L4 by inserts containing two, four, and six glycine residues results in  $\Delta H_m$  values higher than those measured for the WT. The gain in enthalpy in these loop-insert mutants may reflect optimization of existing contacts or the formation of new ones, within or outside L4. Further elongation of the loop does not lead to additional significant changes. Overall,  $\Delta H_m$  decreases by almost 80 kJ/mol between  $\nabla 6$  and  $\Delta 6$ . This decrease, which concurs with decreasing loop length, opposes the measured change in conformational stability of the proteins, which increases as the loop becomes shorter. The gain in stability upon loop shortening must therefore be of an entropic origin.

Increasing loop length leads to deceleration of folding and acceleration of unfolding of the proteins (Table S3 and Fig. 3A and B). In both cases, the plots of the natural logarithms of the rate constants vs. loop length are nonlinear and tend to saturate as the

length of the loop increases. The magnitude of the changes, however, differs considerably between the folding and unfolding reactions. The effect of loop length on the folding rate of the proteins is quite small, with the difference between the fastest ( $\Delta 6$ ) and slowest ( $\nabla 12$ ) variants being about threefold. Such a relatively small effect is in line with results obtained from phi-value analysis (9) and Monte Carlo and MD simulations (10, 16), which indicate that native contacts are mostly absent from L4 in the folding transition state ensemble. By contrast, the changes in the unfolding rates of the proteins extend over a range of  $\sim 250$ -fold. These changes therefore dominate the changes in stability along the loop-length series.

Previous studies conducted on flexible loop regions revealed that the energetic consequences of changing loop length are predominantly related to the entropic cost of ordering a loop upon folding (18–22). This effect can be approximated by simple polymer models of the form

$$\Delta\Delta G(n) = cRT \ln(n/n_{\text{ref}}), \quad [1]$$

where  $n$  denotes the number of residues in the loop of a given variant and  $n_{\text{ref}}$  is the number of residues in the loop of a reference mutant (usually, the one carrying the largest number of residues). The coefficient  $c$  is a correction factor that is related to the persistence length and which depends on the nature of the polymer and on the length and composition (in our case, the amino acid content) of the loop (23, 24). To estimate the contribution of loop closure entropy to the changes in the stability of the hmAcP variants, we used Eq. 1 with two extreme values of  $c$ , one ( $c = 1.5$ ) corresponding to an ideal random-walk chain and the other ( $c = 2.44$ ) taking into account excluded volume effects for both the loop and the residues that flank it (18, 23). The results, depicted in Fig. 4, show that this term can account for only a fraction of the observed differences in thermodynamic stability within the  $\nabla 6$ – $\Delta 6$  range, with the relative contribution becoming increasingly smaller as the length of the loop decreases.

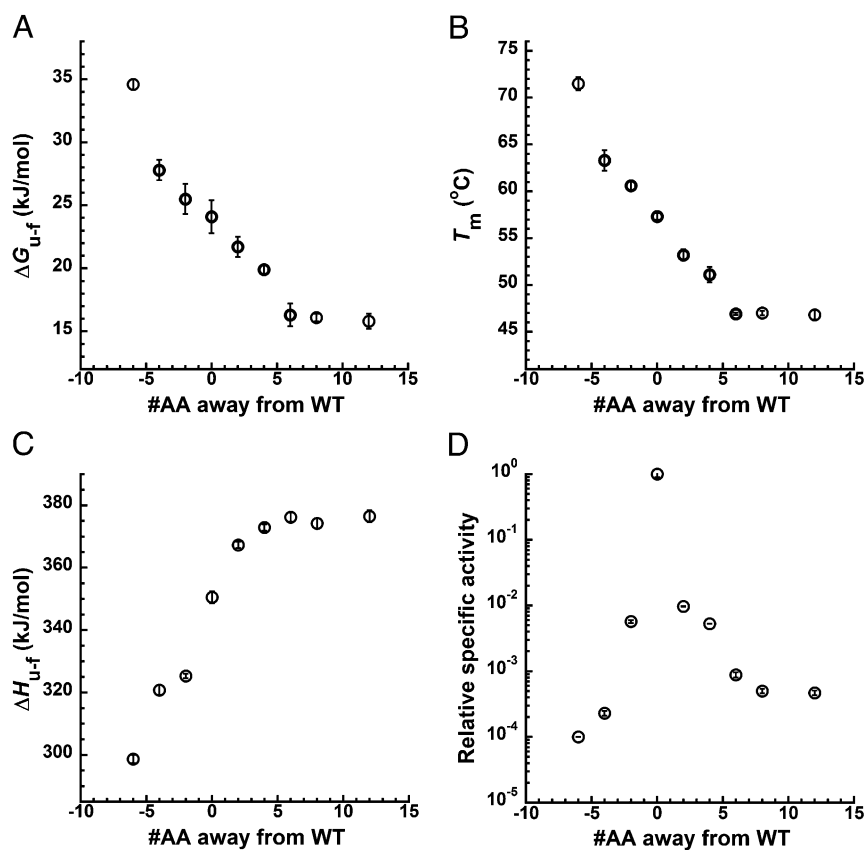
The analysis described above was complemented by native topology-based (Gō-model) simulations. In these studies, the loop-length series was generated by insertions of stretches of C $\alpha$  beads mimicking oligoglycine chains into the loop possessed by the  $\Delta 6$  mutant, which was used as a reference. To isolate topological effects, attractive noncovalent interactions involving residues within the modified loop region were omitted, so that the folded state of all variants is defined by the same set of native contacts. These settings resemble the polymer-based models in the sense that the effects produced by the changes in loop length are mostly confined to the unfolded and transition states. Consistent with the results derived from the kinetic analyses, increasing the length of L4 slowed folding and facilitated unfolding (Fig. S2). However, the magnitude of the effect on the unfolding reaction was not captured by the simulations, which revealed only a twofold increase in the unfolding rate upon elongation of the loop by 26 residues. In both cases, the model predicts a linear dependence of the rate constants on loop length, deviating from the experimentally observed behaviors.

What, then, is responsible for the surplus entropic stabilization of the proteins within the  $\nabla 6$ – $\Delta 6$  range when the length of L4 is decreased? The data presented so far strongly indicate that the effect is related to the properties of the folded state. One such property is configurational entropy: If shortening of L4 leads to an increase in the entropy of the folded state, it may stabilize the proteins by decreasing the entropic gain of unfolding. To test this possibility, we performed all-atom MD simulations on the WT protein and the  $\Delta 6$  mutant. We first addressed the structural consequences of the deletion. The matrix shown in Fig. 5A represents the differences in interresidue distances between the two proteins ( $\langle d_{ij}^{\Delta 6} \rangle - \langle d_{ij}^{\text{WT}} \rangle$ ), where  $\langle d_{ij} \rangle$  is the mean pairwise distance

**Table 1.** Loop-length variants used in this study

Variant	Sequence of L4
$\Delta 6$	WLSKVG-----DR
$\Delta 4$	WLSKVGs----IDR
$\Delta 2$	WLSKVGSP--RIDR
WT	WLSKVGSPSSRIDR
$\nabla 2$	WLSKVGSPS <b>GG</b> SRIDR
$\nabla 4$	WLSKVGSPS <b>GGGG</b> SRIDR
$\nabla 6$	WLSKVGSPS <b>GGGGGG</b> SRIDR
$\nabla 8$	WLSKVGSPS <b>GGGGGGGG</b> SRIDR
$\nabla 12$	WLSKVGSPS <b>GGGGGGGGGG</b> SRIDR

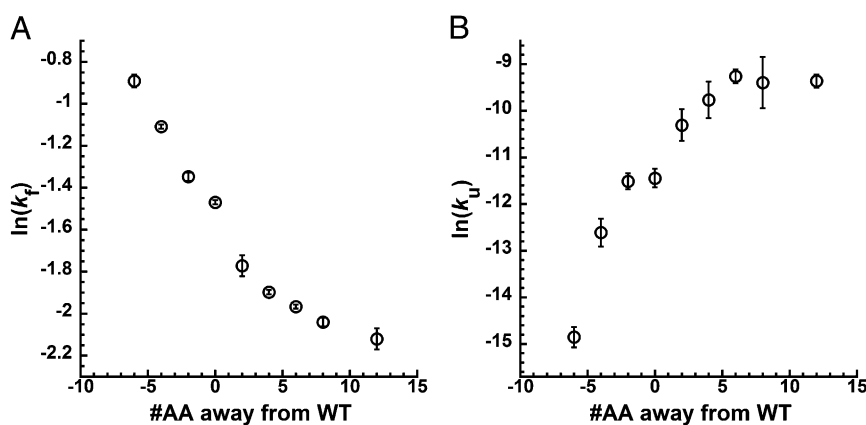
Boldface indicates glycine residues.



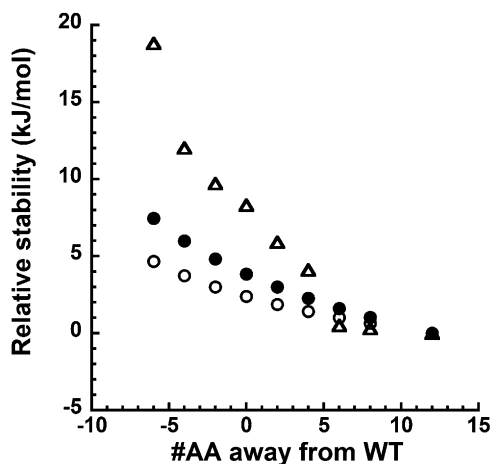
**Fig. 2.** Effects of L4 length on hmAcP stability and activity. The x-axes denote the difference in the number of residues in L4 between the loop-length mutants and the WT. (A) Unfolding free energy (25 °C). (B) Midpoint temperature of unfolding. (C) Calorimetric unfolding enthalpy. (D) Specific activity (25 °C). The values in D were normalized with respect to the activity of the WT protein. The data shown in this figure, as well as in Fig. 3, represent the means  $\pm$  SD of at least three independent determinations.

between the  $C\alpha$  atoms of residues  $i$  and  $j$ ) derived from analysis of 1,500 snapshots observed during 10 20-ns runs. The major differences relate to residues located within L4 and L1, and the helix adjacent to L1,  $\alpha 1$ . They amount to a small shift in the position of  $\alpha 1$  (which also becomes slightly kinked) in the mutant, which moves  $\alpha 1$  away from the  $\beta$ -sheet as well as from the second helix ( $\alpha 2$ ). The shift is induced by a conformational change in L1, which results in a movement of its C terminal toward L4. This repositioning is enabled in  $\Delta 6$  because the  $\beta$ -bulge in L4 that lies below L1 is removed by the deletion. Overall, however, the structure of the two proteins is

similar, consistent with the far-UV CD and fluorescence emission data. This is further supported by near-UV CD analysis, which is extremely sensitive to changes in the microenvironment around aromatic residues. As can be seen (Fig. S1B), the major difference between the spectra recorded for the WT and  $\Delta 6$  is a lower amplitude of the signal up to  $\sim 275$  nm in the spectrum of the latter, but the positions of the maxima and minima are conserved. The decrease in the amplitude at short wavelengths may reflect perturbations of interactions between L4 and Tyr25 in  $\alpha 1$  (our own contact analysis) and/or change in the distance ( $d_{wt} = 2.75$  Å) between



**Fig. 3.** Dependence on L4 length of folding (A) and unfolding (B) rates, measured at 25 °C.



**Fig. 4.** Changes in stability predicted by the loop entropy model, using  $c$  values of 1.5 (○) and 2.44 (●). The experimentally determined differences in unfolding free energy are marked by (△). Values were normalized with respect to the stability of the  $\nabla 12$  mutant.

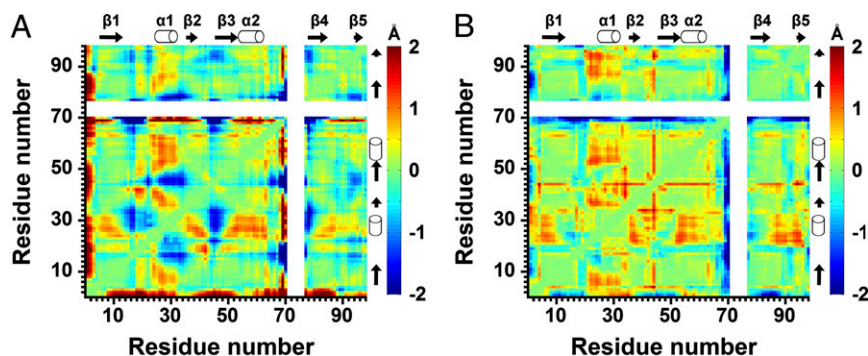
Tyr25 and Trp64 in L4. As discussed below, it may also reflect the altered dynamics of the folded state of the mutant. The differences between the spectra recorded for the other deletion mutants and the WT are even smaller (Fig. S1B).

Next, we examined the impact of the six-residue truncation in L4 on the conformational flexibility of the protein. Fig. 5B shows the differences in the SDs of the interresidue distances between  $\Delta 6$  and the WT. The matrix reveals that the variance of the distances is generally higher in the mutant. The most prominent increases are apparent in regions corresponding to distances between residues located in L1 (C terminal) and  $\alpha 1$  and residues in  $\alpha 2$ , the first ( $\beta 1$ ), second ( $\beta 2$ ), third ( $\beta 3$ ), and fifth ( $\beta 5$ ) strands of the sheet, and the loop that connects the fourth strand ( $\beta 4$ ) to  $\beta 5$ . These increases most likely result from the removal of the  $\beta$ -bulge in L4 and the breakage of hydrogen bonds it makes with L1 by the deletion, lessening restrictions on the motion of L1 and the adjacent helix. Other, more localized, increases are observed for residues located in  $\alpha 2$  and the  $\beta$ -turn connecting strands 2 and 3. An opposite effect is exhibited mainly by residues located at the edges of L4, particularly at the N terminal, for which the SDs are mostly lower in the mutant. Notably, albeit being overall more flexible,  $\Delta 6$  has, on average, a smaller solvent-accessible surface area (Fig. S3). Results obtained from experiments using the fluorescence probe 8-anilino-1-naphthalene sulfonate (ANS) are in line with this notion, showing that binding of the dye to the loop-length variants

decreases with decreasing loop length (Fig. S1D). These results are consistent with the decrease observed between  $\Delta 6$  and  $\nabla 6$  in the  $m$ -values (Tables S2 and S3), which correlate to the difference in the accessible surface area between the folded and unfolded states (refs. 25–29 and references therein).

To quantify the differences apparent in Fig. 5B, we followed ref. 30 (see also ref. 31) and used the covariance matrices of the atomic fluctuations observed in the MD trajectories to estimate the configurational entropy of the folded state ensemble of the two proteins. The analysis yielded values of 1.61 and 1.72 kJ/mol-K for WT and  $\Delta 6$ , respectively. At 25 °C, the consequence of this difference in internal entropy is stabilization of the folded state of  $\Delta 6$  over that of the WT by 32.8 kJ/mol—almost an order of magnitude larger than the stabilization conferred by the corresponding difference in loop closure entropy (3.63 kJ/mol, with  $c = 2.44$ ). Using Kirchhoff's relation, the folding enthalpies of the WT and  $\Delta 6$  at 25 °C are estimated to be *ca.* -151 and -127 kJ/mol. Given this and the differences in configurational and loop closure entropies, the  $\Delta 6$  mutant is expected to be stabilized (at 25 °C) by  $\sim 12$  kJ/mol compared with the WT, not too far from the experimentally determined difference of 10.5 kJ/mol (Table S2). Further analysis reveals that the secondary structure that contributes the most to the increase in the configurational entropy of  $\Delta 6$  is  $\alpha 2$  (Table S4). The first helix,  $\beta 3$ , and  $\beta 4$  each contributes less than 50% compared with  $\alpha 2$ ; contributions made by  $\beta 1$ ,  $\beta 2$ , and by the catalytic loop (L1) are yet smaller, in the latter case likely reflecting the high flexibility of this loop in the native protein in the absence of ligand (4). The terminal strand of the sheet ( $\beta 5$ ) is found to be more restricted in the mutant than in the WT. Separating the contributions of backbone and side-chain atoms to the overall increase in folded state entropy of the mutant, we found the relative weight of backbone disordering to be similar to or larger than side-chain mobility for  $\alpha 1$ ,  $\alpha 2$ ,  $\beta 2$ , and L1. This is reversed in the first, third, and fourth strands of the sheet, where side-chain mobilization makes a comparatively larger contribution.

The catalytic pocket of hmAcP is located in a cleft between L1 and the  $\beta$ -turn connecting  $\beta 2$  and  $\beta 3$ , which lies above L1 (Fig. 1). L1 adopts a cradle-like conformation, characteristic of phosphate-binding pockets, and functions in the binding of the phosphate moiety of the substrate and the stabilization of the transition intermediate. The active site is completed by a conserved arginine residue (Arg23), located at the interface between L1 and  $\alpha 1$ , which serves as the primary binder of the substrate phosphate group, and by an asparagine residue (Asn41), located in the  $\beta$ -turn, which binds the catalytic water molecule (4, 12–15). As shown in Fig. 2D, alterations in L4 length, caused either by deletion or by insertion of residues, lead to a marked decrease in enzymatic activity. As was observed for the thermodynamic and kinetic parameters, the effect is sharper and more extensive in the deletion mutants.



**Fig. 5.** Differences in mean interresidue distances ( $\langle d_{ij}^{\Delta 6} \rangle - \langle d_{ij}^{WT} \rangle$ ) (A) and their SDs ( $SD d_{ij}^{\Delta 6} - SD d_{ij}^{WT}$ ) (B) between  $\Delta 6$  and WT hmAcP, as derived from analysis of snapshots from all-atom MD simulations. The white areas correspond to residues in L4 that are absent in the mutant. Secondary structures (defined by DSSP):  $\alpha 1$  (residues 25–33),  $\alpha 2$  (residues 55–63),  $\beta 1$  (residues 6–14),  $\beta 2$  (residues 36–40),  $\beta 3$  (residues 46–54),  $\beta 4$  (residues 78–85), and  $\beta 5$  (residues 94–97).



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