Capillarity theory for the fly-casting mechanism

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Biomolecular folding and function are often coupled. During molecular recognition events, one of the binding partners may transiently or partially unfold, allowing more rapid access to a binding site. We describe a simple model for this fly-casting mechanism based on the capillarity approximation and polymer chain statistics. The model shows that fly casting is most effective when the protein unfolding barrier is small and the part of the chain which extends toward the target is relatively rigid. These features are often seen in known examples of fly casting in protein–DNA binding. Simulations of protein–DNA binding based on well-funneled native-topology models with electrostatic forces confirm the trends of the analytical theory.

binding mechanism | disordered proteins | fast folding | protein folding

It is becoming clear that protein folding and protein functioning are often overlapping processes. For cooperatively folding proteins, a free energy barrier separates the folded configurations from the unfolded ones. If this barrier is sufficiently high, we expect the traditional "function follows folding" paradigm to be valid. Many proteins however are unfolded before they function (1–5). Other proteins have native ensembles separated by only a small barrier from their disordered states. It has recently been argued that in some circumstances there may be no folding barrier at all (6–8). Clearly in all these cases folding and function must be coupled. In addition, partially surmounting the folding barrier, even if it is high, may short circuit the otherwise large barriers that would accompany allosteric changes, if the protein were required to always remain intact. These two ways of coupling the folding landscape and the functional landscape have been termed "fly casting" (9–11) (for the binding process) and "cracking" (for allosteric change) (12–14). In the fly-casting scenario, a protein may bind from a relatively large distance, thereby enhancing its capture radius: The tradeoff is between the entropy cost from extending a subdomain and the energy gained upon binding to a target. Although the disordered proteins may have slower translational diffusion comparing to globular proteins, their intrinsic flexibility imposes fewer constraints on binding and therefore they may have faster binding to their binding partners (10, 15). It is possible that the biological function of downhill and ultrafast folding (16–20) is to achieve fast binding via fly casting. In this paper, we explore the interplay between the fly casting and the folding barrier using the capillarity model for protein folding, which in its simplest form ignores many of the structural features of the native protein.

Despite the intrinsic complexity of the folding of a random heteropolymer, most proteins have evolved to fold via a funneled energy landscape (21, 22). This evolved feature greatly simplifies the physics of the folding process because the primary free energy scales involved are then the entropy of organizing the chain into a specific topology and the stabilization energy. These free energies must balance near the physiological folding temperature, giving a single parameter that determines the specific topology free energy profile. The remaining smaller energy scales come from the ruggedness of the landscape (which is reflected in the rate of conformational diffusion) across the landscape and a cooperativity energy that comes from the nonadditivity of interresidue forces which has a large component from solvation. The latter effect is very analogous to the surface tension of a liquid condensing from a gas. The capillarity picture of folding takes over the picture of nucleation at a first-order transition more or less intact to describe the change from folded to unfolded states (23, 24). This picture might be called the "spherical cow" approximation to folding because it ignores, to zeroth order, the specifics of protein topology and connectivity. This great oversimplification is, however, a positive feature when we wish to understand trends, such as the scaling of folding rate with length, etc.

In this paper, we use the capillarity picture to look at fly casting. The model gives crisp criteria for the conditions under which fly casting can occur. The analysis shows the key role played by the ratio of the binding affinity to the folding barrier in determining whether fly casting will occur. In general, fly casting is encouraged by high affinities and low barriers. Fly casting and cracking are thought to play a special role in how transcription factors navigate along DNA and brachiate between DNA chains (25). On the basis of the present theory, it turns out then to be quite natural that DNA binding proteins have been found to be among the fastest folders (10, 17). Rigidity of the protein in the denatured state also encourages fly casting, thus suggesting an increased possible role for residual structure in the denatured state.

In addition to outlining the capillarity model of fly casting in this paper, we compare the theory with results from a topology-based simulation model of the protein–DNA binding process. This analysis confirms the trends expected from the capillarity model.

Methods

Capillarity Model of Fly-Casting Association. For our purposes, the protein made up of N residues is split into three regions (see Fig. 1). The first part with N_1 residues is structured (i.e., folded) and in contact with the target (assumed to be a relatively simple geometry, such as an interface, membrane, or DNA). At the other terminus of the protein, we have another structured region of N_2 residues. Finally, the fly-casting effect translates into an intermediate region with $N_3 = N - N_1 - N_2$ unstructured residues, with end-to-end extension L, and perpendicular to the binding substrate. This intermediate section will be treated as a standard homopolymer coil under stretching. The N_1 section being in direct contact with the target, the protein center-of-mass distance to the substrate is $R = L(N_2 + N_3/2)/N$. We implicitly neglect the size of ordered regions (one and two) compared to the "arm" extension L, and we emphasize that the conformations under study here impose a contact between the protein and the binding substrate.

Under those assumptions, the total free energy is written as

$$F = F_{cap}(N_1) + F_{cap}(N_2) + F_{bind}(N_1) + F_{ent}(N_3) \qquad [1]$$

Both N_1 and N_2 termini contribute to the free energy through a capillarity term (23, 24)

$$F_{cap}(N_i) = \gamma(N_i^{2/3} - N^{-1/3}N_i) + \tau N_i \qquad [2]$$

where $\tau \propto T - T_f$ denotes the deviation from folding temperature T_f. The quantity γ is analogous to a surface tension. At T_f, it is the single parameter that governs the free energy barrier to completely fold the protein
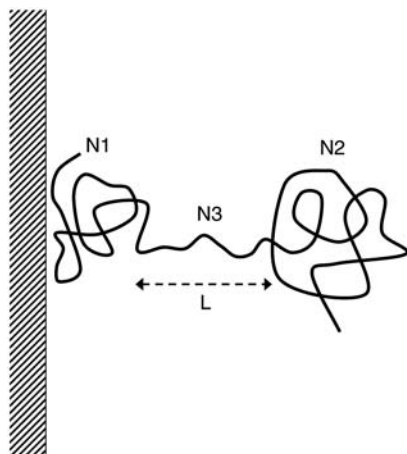
Fig. 1. Schematic view of a protein that interacts with a target (illustrated by the flat surface) via the fly-casting mechanism. The protein is composed of three regions: two folded regions, $L1$ and $L2$, and a flexible linker of length $L3$.

$$F_{\text{cap}}^{\text{barrier}} = \frac{4\gamma N^{2/3}}{27(1 - \tau N^{1/3}/\gamma)^2} \qquad [3]$$

In what follows, we will refer to the free energy barrier for folding as the above quantity, evaluated at folding temperature

$$B = \frac{4\gamma N^{2/3}}{27} \qquad [4]$$

If ν denotes the Flory exponent (26) of the intermediate N_3 part, the corresponding entropy cost of stretching reads $F_{\text{ent}}(N_3)$, up to an irrelevant prefactor

$$F_{\text{ent}} \propto kT\varepsilon \left(\frac{L}{aN_3^\nu}\right)^{1/(1-\nu)}, \qquad [5]$$

where a denotes the residue size (approximately 0.3 nm), and kT is the thermal energy. Whether we consider a Gaussian chain ($\nu = 1/2$) or a swollen coil with excluded volume ($\nu \approx 0.6$) is immaterial, and we will assume for simplicity that $\nu = 1/2$ in the following. More important is the prefactor ε that accounts for the rigidity of the chain. It can be viewed as the ratio a/l_p where l_p is the chain persistence length: $\varepsilon = 1$ for a fully flexible chain, whereas we will consider $\varepsilon = 0.2$ for a typical protein. Finally, as far as the binding term is concerned, several models can be considered; in the simplest approximation, we shall take $F_{\text{bind}}(N_1) = -\delta N_1 kT$. Several constraints should be enforced, such as $L \leq N_3 a$ or others resulting from working at fixed R.

Simulation Model of Biomolecular Association. We study the effect of the folding barrier and binding affinity on the fly-casting characteristics using a coarse-grained simulation model for a system that has been reported to follow the fly-casting mechanism. The association of the Ets protein to its specific DNA binding site was studied using a native-topology-based model (Go model) supplemented by electrostatic interactions. The native-topology-based model takes into account only interactions that exist in the native structure and, therefore, includes mainly topological frustration. Adding nonspecific electrostatic interactions contributes energetic frustration between the protein and the DNA as well as within the protein. Purely structure-based models have already been used to study the folding of many monomeric proteins that fold in a two-state fashion (27–30) or that fold via a more complicated folding scheme. They have also been used to study higher molecularity reactions such as dimerization and tetramerization (11, 31–33).

In our study, the protein and the DNA are modeled using a reduced representation. Each residue is represented by a single bead centered on its α-carbon (C_α) position. Adjacent beads are strung together into a polymer chain by means of a potential encoding bond length and angle constraints. The secondary structure is encoded in the dihedral angle potential and the nonbonded (native contact) potential. In the framework of the model, all native contacts are represented by a 10–12 Lennard Jones form without

any discrimination between the various chemical types of interaction. The residues do not have any chemical identity (the information for folding is encoded in the structure) but some have a point charge. Accordingly, positively charged residues (Arg and Lysine) have positive point charge and the negatively charged residue (Asp and Glu) have a negative point charge. The other beads are neutral. Details of the coarse-grained modeling of the protein–DNA system can be found in previous publications (10, 34).

To enhance the sampling of binding events, a constraint is applied on the protein–DNA system so that they are confined to a sphere of radius 40 Å centered at the center of mass of the DNA that is kept frozen. For each electrostatic strength, several constant temperature molecular dynamics simulations were performed starting from an unbound (folded or unfolded) protein conformation. At a given temperature, several trajectories were collected starting from different initial conformation and velocities. The length of the simulations was determined by the demand of having several transitions of folding/unfolding or binding/unbinding at the transition temperatures. The multiple trajectories were combined using the Weighted Histogram Analysis Method (35) to calculate thermodynamic properties of the systems.

To investigate the effect of the folding barrier of Ets and its affinity to DNA, the association of Ets with its DNA cognate was studied for different values of dielectric constant. In addition, the folding barrier was tuned by increasing the cooperativity by incorporating a nonadditive term to the Hamilitonian (36).

Results

Persistent Limit. The case of a persistent fly-casting arm is straightforward to work out and yields an interesting benchmark. In this limit indeed, the ratio ε is small, and the entropy cost of the arm irrelevant. We therefore assume here that the middle part of the protein is fully stretched, so that $L = N_3 a$, which therefore provides the most favorable conditions for the occurrence of fly casting. It can be shown that, whenever the total free energy F becomes negative, the only folded region of the protein is that part in contact with the membrane ($N_2 = 0$) and N_1 takes its maximum value allowed (for a given value of R): $N_1 = N - \sqrt{2NR/a}$. Starting from a large value of R, F first increases upon decreasing R, which corresponds to the energy penalty of folding of N_1-like units, then decreases and vanishes at $R = R^*$ with

$$R^* = \frac{1}{2}\left[\left(1 + \frac{\delta N^{1/3}}{\gamma}\right)^{-3} - 1\right]^2 \qquad [6]$$

For $R < R^*$, $F < 0$; of course, the states with positive free energy at $R > R^*$ are metastable and are obtained enforcing a contact between the protein and the binding substrate for all admissible R. As a consequence, in the range $R > R^*$, it is more favorable to approach the substrate in the collapsed state (with $N_1 = N_2 = 0$), with a vanishing free energy and no contact to the substrate. The free energy profile is shown in Fig. 2.

Increasing the ratio δ/γ increases R^*, but preserves the shape of the curves shown in Fig 2. Although it is thermodynamically favorable to fly cast when $R < R^*$, kinetic effects may preempt the phenomenon, and it is of interest to compute the associated free energy barrier. To this end, we notice that, as far as the folding of N_1 residues is concerned, a folding temperature mismatch τ without binding is equivalent to a (negative) binding term at the folding temperature; taking advantage of this $\delta \leftrightarrow -\tau$ correspondence, Eq. **3** yields an energy barrier

$$F_{\varepsilon=0}^{\text{barrier}} = \frac{4\gamma N^{2/3}}{27(1 + \delta N^{1/3}/\gamma)^2} < B \qquad [7]$$

If the quantity on the left-hand side above exceeds some threshold F^{thres}, fly casting will not take place. More explicitly, such a situation of kinetic hindrance occurs for $F^{\text{thres}} < B$ under the condition that for

Fig. 2. Persistent limit $\varepsilon = 0$. (*A*) F/B as a function of center of mass distance R to the substrate. Here, B denotes the barrier for folding defined in ref. 4, i.e., in the absence of binding; we took $B = 5kT$, $N = 100$, $\delta = 0.1$ (which corresponds to a binding energy of $-10kT$). The value of R where F vanishes defines R^* (see the arrow) and discriminates the states with positive free energies at $R > R_*$ (shown with a dashed line) from the stable ones with $R < R_*$. Consequently, the most stable configuration when $R > R_*$ is for a protein "detached" from the substrate, which can be either a disordered state or the folded state (assuming we are at the folding temperature). Hence, the optimal free energy profile is the one shown by the thick continuous line. For the parameters chosen, Eq. **6** gives $R^* = 0.15Na$, which is indeed observed in the figure. Taking for concreteness a residue size of 0.3 nm, this corresponds to $R^* = 4.5$ nm. (*B*) Plot of the number of residues in the region in contact with the substrate, as a function of R, for the same parameters as in (*A*). Metastable states are again shown by the dashed lines, whereas the stable states correspond to the thick continuous curve.

$$\delta NkT < \frac{27}{4} B \left(\sqrt{\frac{B}{F^{\text{thres}}}} - 1 \right) \qquad [8]$$

In the remainder, we will refer to δNkT as the affinity.

General Case ($\varepsilon \neq 0$). For a given value of R, the free energy in Eq. **1** depends on two variables (e.g., N_3 and L), whereas N_2 follows from $R = L(N_2 - N_3/2)/N$ and $N_1 = N - N_2 - N_3$. At variance with the persistent limit where the arm extension L can take its maximum value (N_3a) at no entropy cost, L is here a variable that follows from minimizing the total free energy. In the relevant parameter range, at fixed R and L, $F(N_3)$ is a concave function, which therefore reaches its minimum at the boundaries of the accessible N_3 domain. This simplifies the analysis when it comes to finding the optimal L for a given center-of-mass distance R. Once the resulting function $L(R)$ is known, we can compute the fly-casting distance R^* for which F becomes negative.

In Fig. 3, the critical fly-casting distance corresponding to the onset of negative free energies is $R^* \approx 0.042Na$, whereas the cor-

responding value of N_1 is $N_1^* \approx 0.60$. Increasing the barrier for folding B from $5kT$ to $10kT$ significantly reduces R^* to 0.022 (see also Figs. 4 and 5), with $N_1^* \approx 0.75$. On the other hand, decreasing the rigidity parameter ε from 0.2 to 0.1 facilitates fly casting ($R^* \approx 0.06Na$ with nevertheless $N_1^* \approx 0.60$, almost unaffected), keeping γ and δ as in Fig 3.

It turns out that the states that minimize the free energy for $R < R^*$ are such that N_3 (number of residues in the arm; see Fig. 1) takes its maximum value and that, in addition, N_2 vanishes. This latter fact allows one to easily relate the temperature dependence in our model (all figures shown above are at the folding temperature $T = T_f$) to its δ-dependence. Decreasing T is equivalent to increasing δ; more precisely, a given affinity parameter δ at $T \neq T_f$ (i.e., $\tau \neq 0$) is equivalent to an affinity $\delta - \tau/(kT)$ at $T = T_f$.

Of course, several variants of the present model can be put forward to refine the analysis. Our goal here has been to devise a minimal framework. We have nevertheless checked that the

Fig. 3. Free energy profile versus R for the same parameters as in Fig. 2, but with $\varepsilon = 0.2$ instead of zero. The inset shows the corresponding value of N_1. Metastable states are not displayed.

Fig. 4. Plot of iso lines in (barrier B versus affinity) plot.

Fig. 5. Cuts through the contour plots of Fig. 4. (A) Shows the critical fly-casting distance R^* as a function of barrier for folding B in the main graph (at constant binding energy $\delta N kT = 10 kT$). (Inset) Same, as a function of binding energy, at constant barrier $B = 5 kT$. Here, the rigidity parameter is $\varepsilon = 0.2$. (B) Shows N_1^* as a function of barrier for folding B.

present phenomenology is unaffected by a modification of the binding energy function, so that its N_1 dependence saturates beyond a prescribed threshold.

Comparison to Simulations. We examine the effect of the folding kinetics and of the protein affinity to the target on the existence of fly-casting mechanism using coarse-grained modeling of association of the Ets protein to its specific DNA binding site (Fig. 6A). We have previously shown that the Ets protein binds its cognate DNA sequence via a fly-casting mechanism (10). It was shown that the protein flexibility significantly enhances binding to the DNA comparing to a scenario when the protein binds the DNA as a rigid molecule. The fly casting can be probed by plotting the free energy as a function of the separation distance between the protein and DNA (Fig. 6B). These plots indicated a coupling between folding and protein–DNA assembly, even for weak electrostatic forces, resulting in a change of the capture radius of the target. A sharper decrease of the free energy curve is observed when flexibility and electrostatics are both included in contrast to when electrostatic forces alone guide a rigid protein.

To examine the effect of the folding barrier and affinity to the DNA on the mechanism of protein–DNA association and in particular the onset of fly casting, we study the assembly of the Ets protein with its cognate DNA at various dielectric constants and various folding cooperativity (36). These two parameters affect the height of the free energy folding barrier and the free energy of the bound complex. Increasing the folding barrier by incorporating a nonadditive term in the protein Hamiltonian results in a milder fly-casting effect as reflected by the milder slope of the free energy when plotted along the separation distance of protein–DNA (Fig. 6B). Accordingly, as the folding barrier increases, fly casting takes place only with closer proximity of the protein to the DNA. We probe the fly casting by comparing the distance R^{**} of the free energy curves of protein–DNA assembly at a given energy value (Fig. 6B). We point out that R^* and R^{**} are defined differently, yet both distances indicate stronger fly-casting effect as they are larger.

Fig. 6C illustrates that R^{**} gets smaller as the folding barrier increases for different values of dielectric constants. This observation is in harmony with the capillarity theory prediction shown

Fig. 6. Simulation of fly-casting binding in protein–DNA interactions. The binding of the Ets protein to its cognate DNA was shown by native-topology-based model to follow fly-casting mechanism. (A) The crystal structure of the specific complex of the Ets protein with its cognate DNA (Protein Data Bank code 1BC8). (B) Free energy curves as a function of the separation distance between protein and DNA for simulation with different degree of nonadditivity. Larger nonadditivity results with higher folding barrier. The stars correspond to the R^{**} distances that compare the fly-casting strength. (C) The R^{**} as a function of the free energy height of the folding barrier for different values of dielectric constant of the Coulomb interactions. The barrier height was modulated by the nonadditivity term (36). (D) The R^{**} as a function of binding affinity of the Ets to its cognate DNA.

in Figs. 4 and 5*A*. The coarse-grained model agrees with the analytical model with respect to the effect of the protein–DNA affinity on the fly casting. R^{**} is larger for high-affinity protein-DNA interactions (Fig. 6*D*), similar to the trend shown in Fig. 4. We note that it is not practical to make a one-to-one comparison between the analytical and simulation models due to differences in the two models and their parameterization (e.g., in the analytical model the substrate attraction to the target is short range, whereas it is longer range in the simulations due to electrostatic interaction). Nonetheless, despite the differences between the two models, they concur in the unraveling of the key biophysical parameters that can affect the binding via the fly-casting mechanism.

Conclusions

The conceptual separation often made between folding processes and functional dynamics relies on the idea that there is clear distinction in thermodynamic terms between the two parts of the energy landscape—the denatured and native ensembles. In this paper, we have put mathematical flesh on this notion by using a simple model. The capillarity model of folding was generalized to study the folding–binding process. Criteria describing when transient unfolding dominates the binding mechanism can be explicitly found in this model. The extent of fly casting is shown to depend on the ratio of the binding affinity to unfolding barrier height.

Fly casting is also shown to be encouraged by low chain entropy for the unfolded region reducing the free energy cost of reaching far toward the target. These trends are confirmed in simulations of protein–DNA binding using a well-funneled, structure-based model with structural detail. The predicted criteria for fly casting should be susceptible to test by appropriate protein engineering studies of folding/binding kinetics (37).

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