

Cognitive Synthetic Aperture Radar (CoSAR) Prototype

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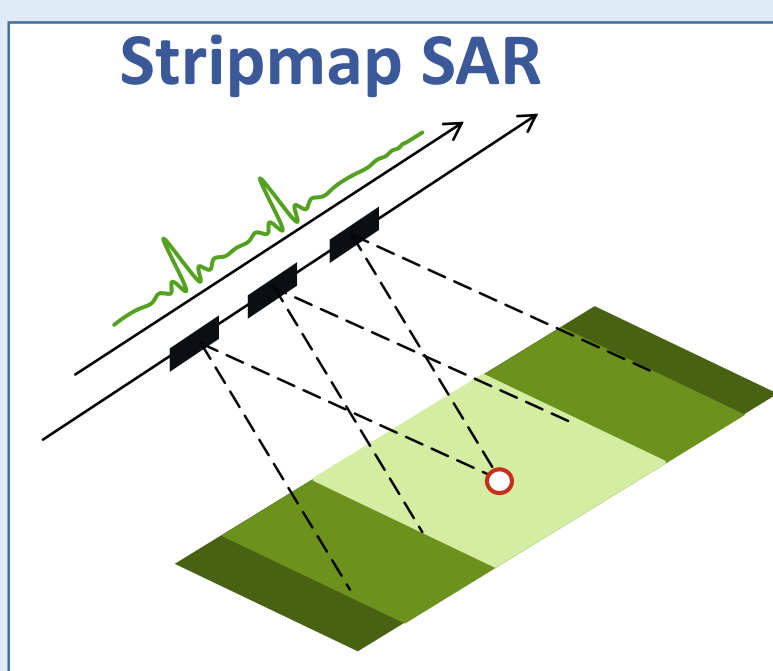
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Main Contributions

- Stripmap synthetic aperture radar (SAR) prototype that demonstrates **sub-Nyquist sampling** in radar imaging and reconstruction of target scene using a **faster 2D recovery** algorithm.
- Cognitive transmission** is employed to further enhance SNR for sub-Nyquist SAR and adaptive frequency allocation.
- Cognitive sub-Nyquist SAR recovers the target scene at low SNRs with **lesser error and greater feature similarities** than non-cognitive Nyquist processing.

Stripmap SAR

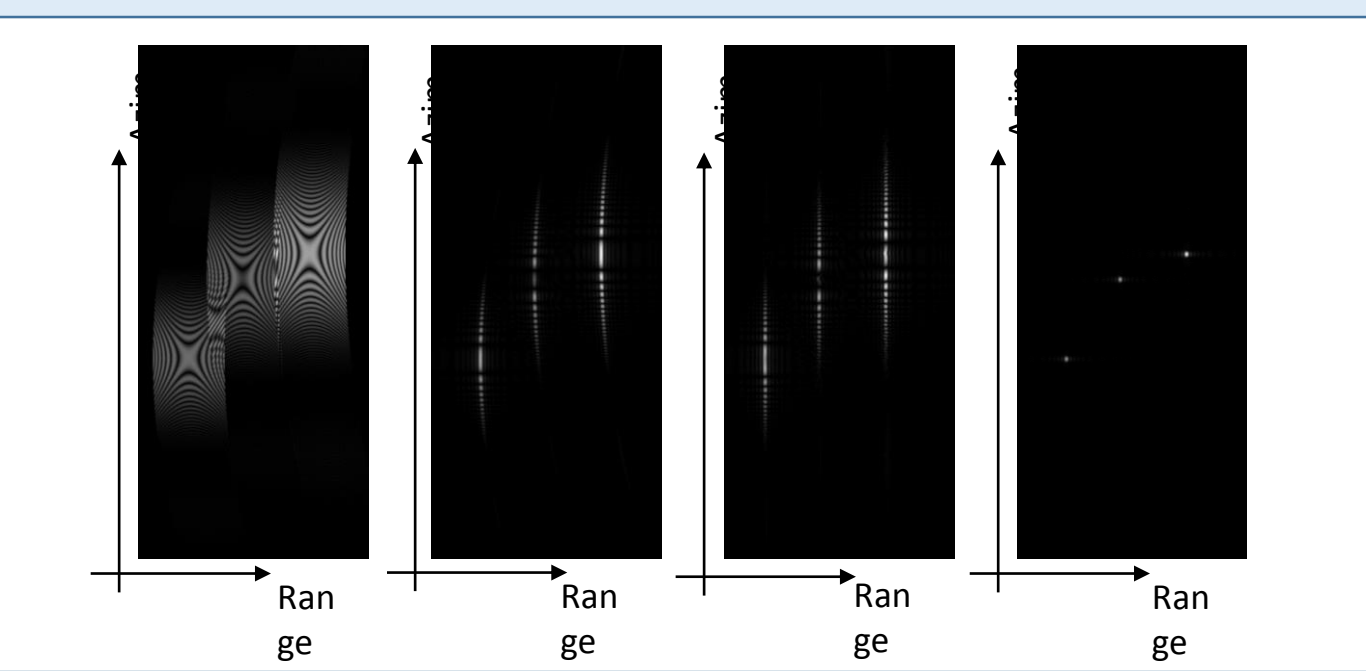
- Conventional SAR strip mapping mode
- A fixed pointing direction antenna broadside to the platform track with the beam pattern:



$$w_a(x_m, r) = \text{sinc}^2\left(\frac{|x - x_m| \cot \frac{\theta_a}{2}}{r}\right)$$

- Strip map is an image formed in width by the **swath of the SAR** and follows the length contour of the flight line of the platform itself.

Range-Doppler Processing



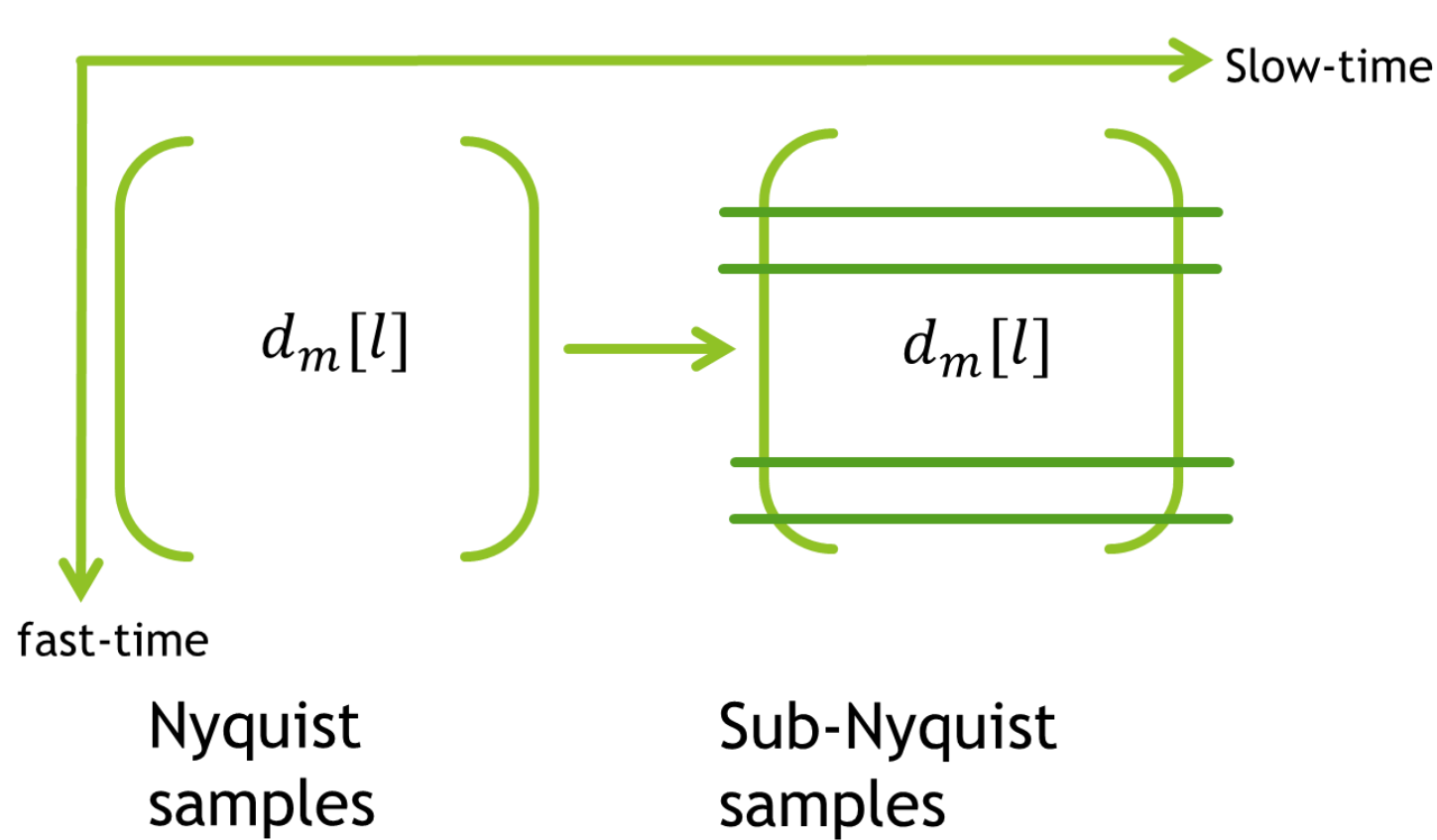
- Range Cell Migration Correction (RCMC) **decouples dependency between the azimuth and range axes** and corrects the hyperbolic trajectory of the targets' echoes.
- RCMC requires digital interpolation **effectively increasing the sampling rate**.

Fourier-Domain Range-Doppler

	Conventional RDA	Fourier Domain RDA
Range Compression	$s[n, m] = d[n, m] * h^*[-n]$	$\tilde{d}_m[l] = T \cdot d_m[l] * h^*[-l]$
Azimuth DFT	$S[n, k] = \sum_{m=0}^{M-1} s[n, m] e^{-j2\pi km}$	$s_k[l] = \sum_{m=0}^{M-1} \tilde{d}_m[l] e^{-j2\pi km}$
RCMC	$\tilde{S}[n, k] = S[n + n \cdot ak^2, k]$	$c_k[l] = \sum_{m \in \text{vec}(k)} s_k[m] Q_{k,2}[-n]$
Azimuth Compression	$Y[n, k] = \tilde{S}[n, k] e^{-j\pi k^2 n}$	$Y[n, k] = \left(\sum_{m \in \text{vec}(k)} c_k[m] e^{j2\pi km} \right) \left(e^{-j\pi k^2 n} \right)$
Azimuth IDFT	$I[n, m] = \frac{1}{M} \sum_{k=0}^{M-1} Y[n, k] e^{j2\pi km}$	$I[n, m] = \frac{1}{M} \sum_{k=0}^{M-1} Y[n, k] e^{j2\pi km}$

- Fourier domain RCMC is similar to beamforming in frequency
- Interpolation is replaced by a weighted sum of Fourier coefficients (weights are characterized by a rapid decay)
- No over-sampling required at the receiver

Sub-Nyquist SAR



- The returned echoes are sampled in the Fourier domain under the Nyquist rate using Xampling
- Xampling requires analog pre-processing

Fast 2D Recovery

- Having the partial Fourier processed measurements, C_p , the image, I , is reconstructed by solving the optimization problem:

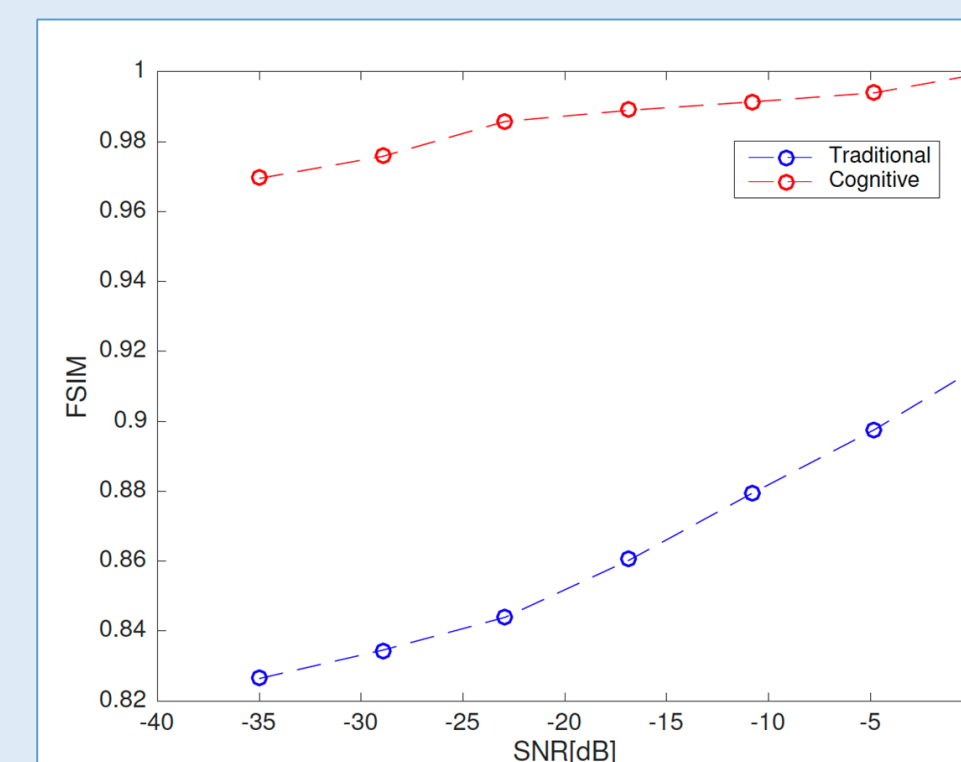
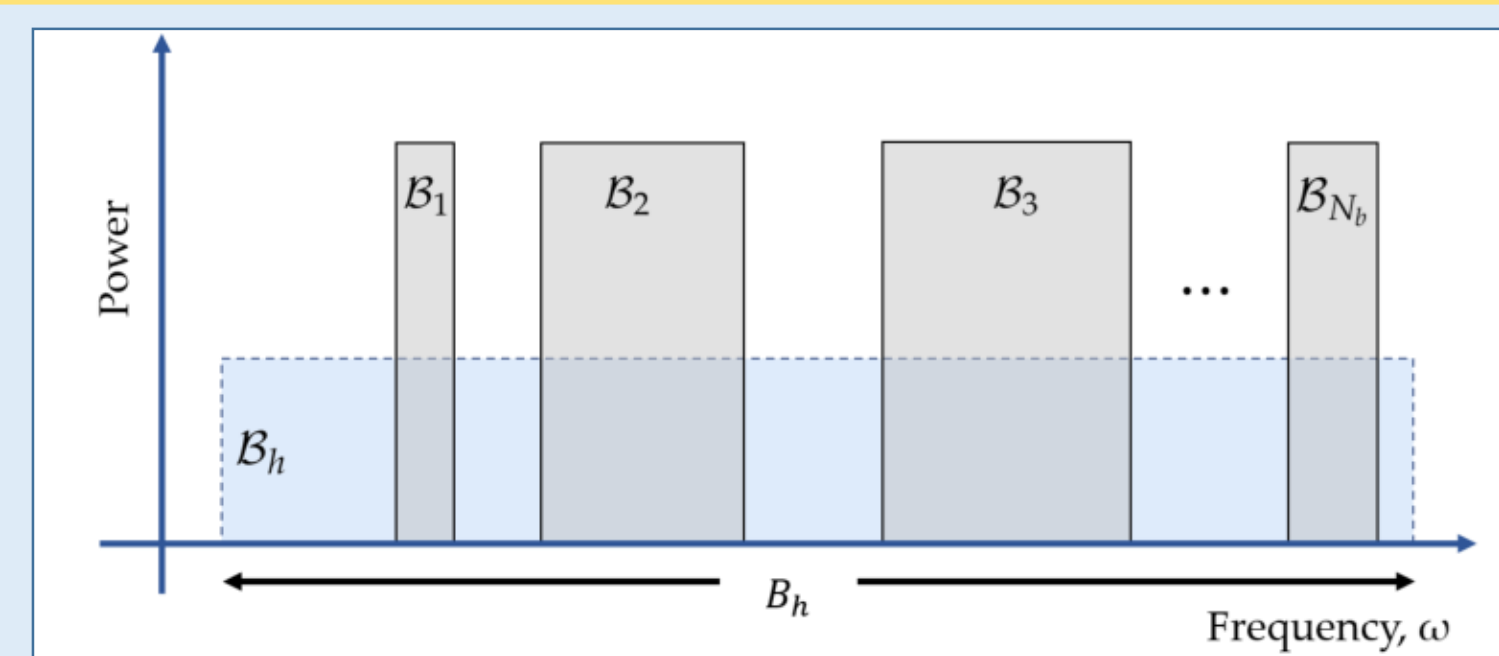
$$\min \| \Psi(I) \|_1 \text{ s.t. } \| C_p - F^S_p [B \circ (IF)] \|^2 < \epsilon$$

F – DFT matrix
 F^S – Sampled Fourier series transformation
 B – Azimuth Compression matrix
 Ψ – Sparsifying transform

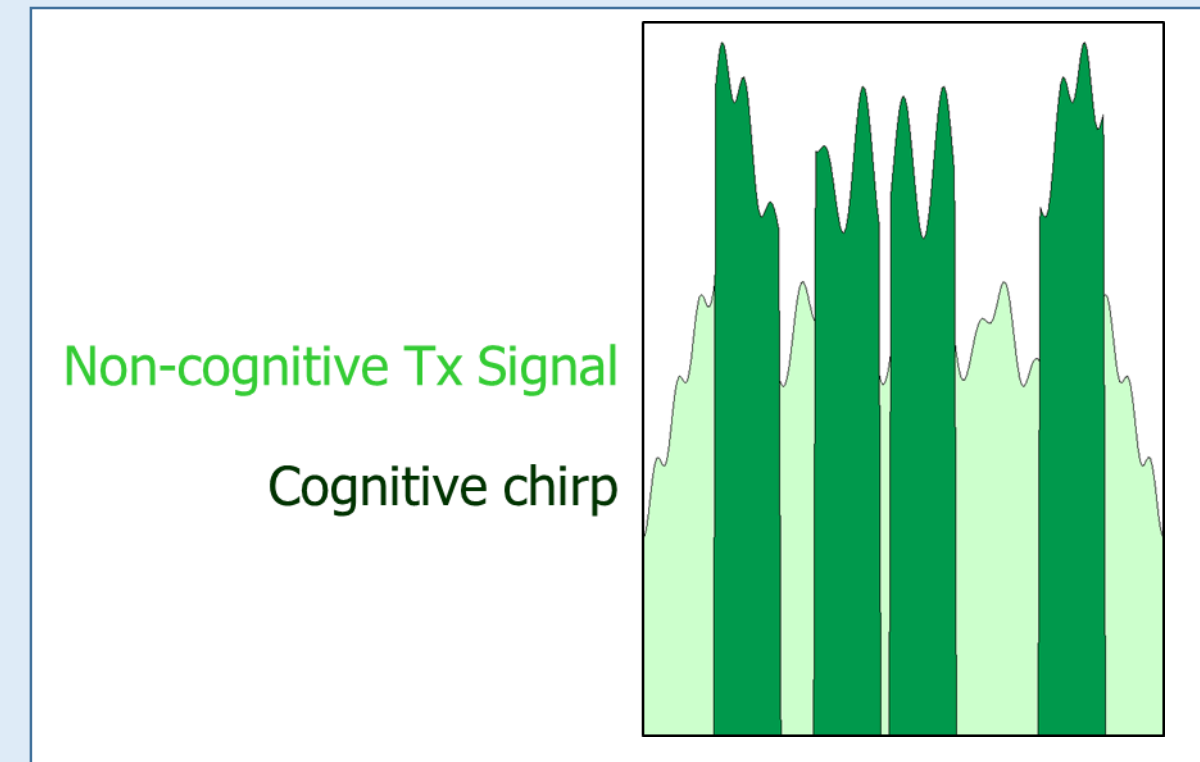
- Recovery by extended Fast Iterative Soft Thresholding Algorithm (FISTA)

Cognitive SAR (CoSAR)

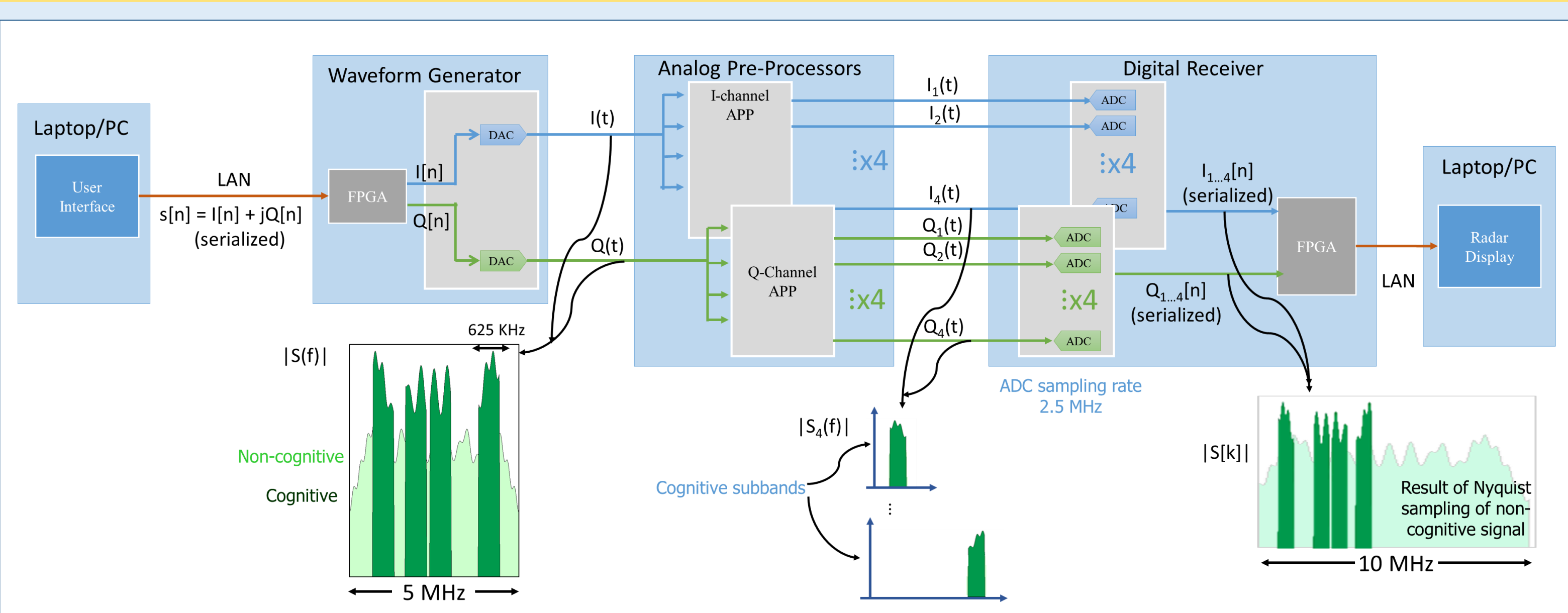
- Cognitive SAR sub-Nyquist receiver design
- CoSAR transmits only in a few narrow disjoint subbands
- A framework for adaptive transmission and reception of SAR signals



All Tx power can be focused in narrower bands → high SNR



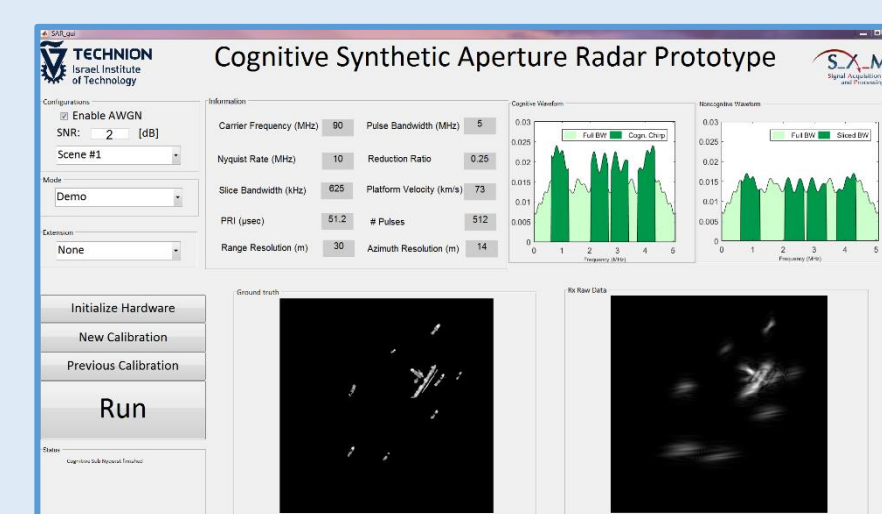
CoSAR System Design



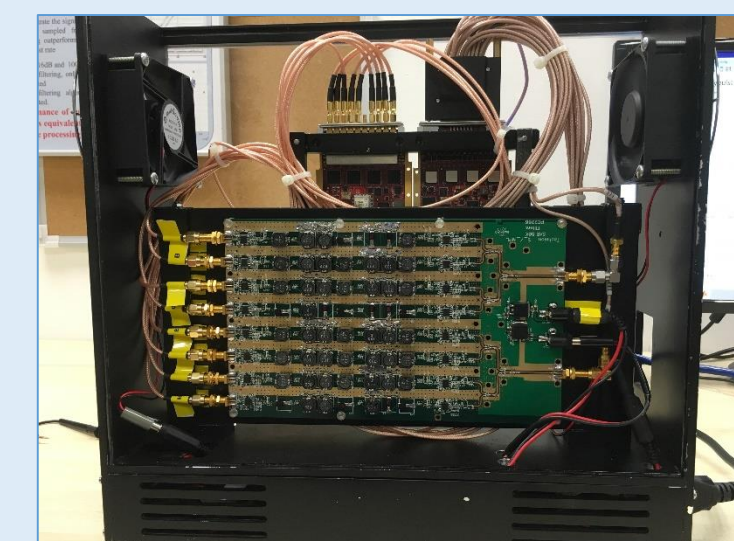
- 5 MHz cognitive chirp
- 4 subbands of 625 kHz bandwidth
- Xampling at 1/4th of the Nyquist rate
- RCMC at 1/8th of the Nyquist rate

CoSAR Submodules

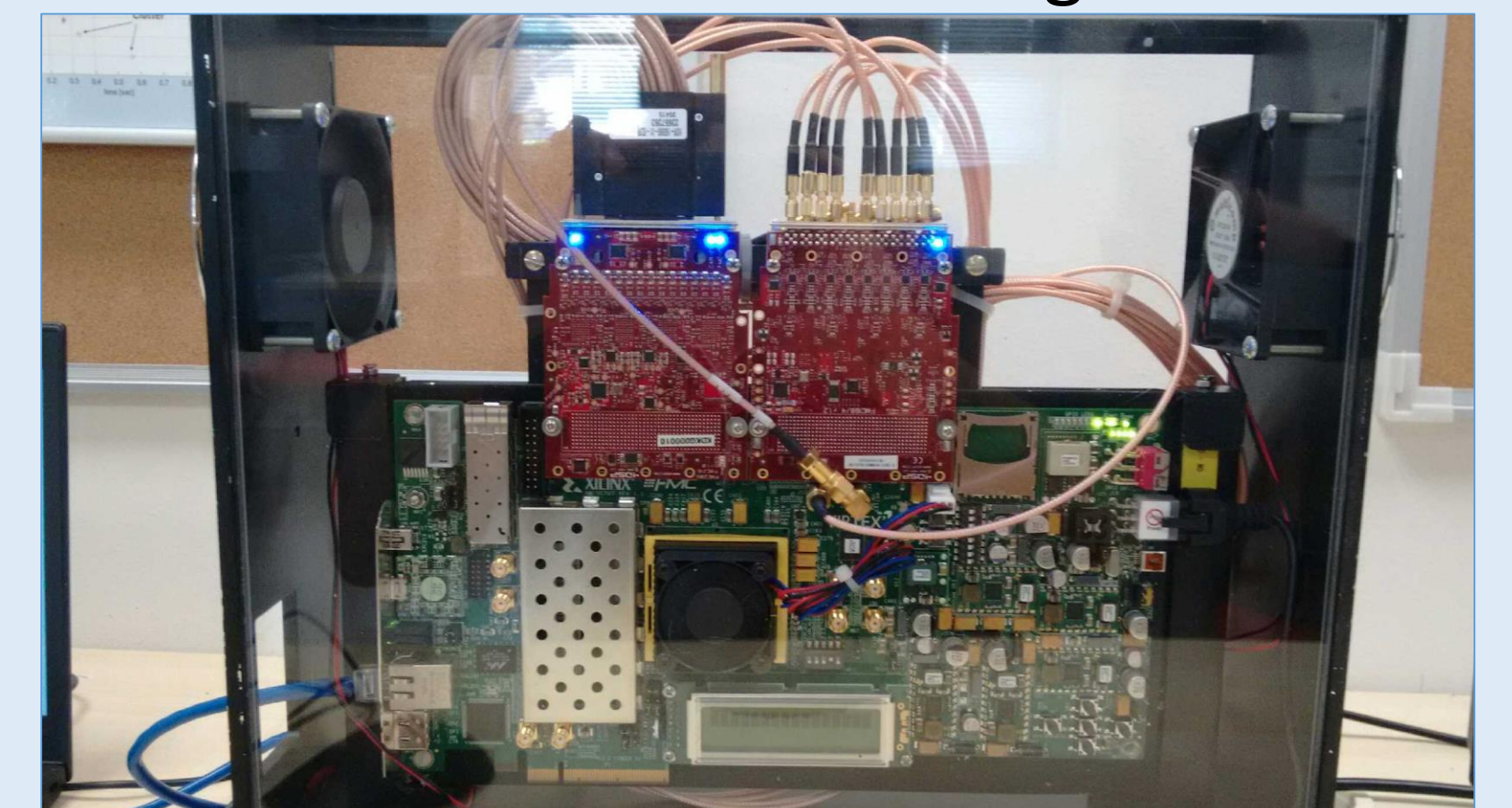
Radar Controller



Analog Pre-Processor

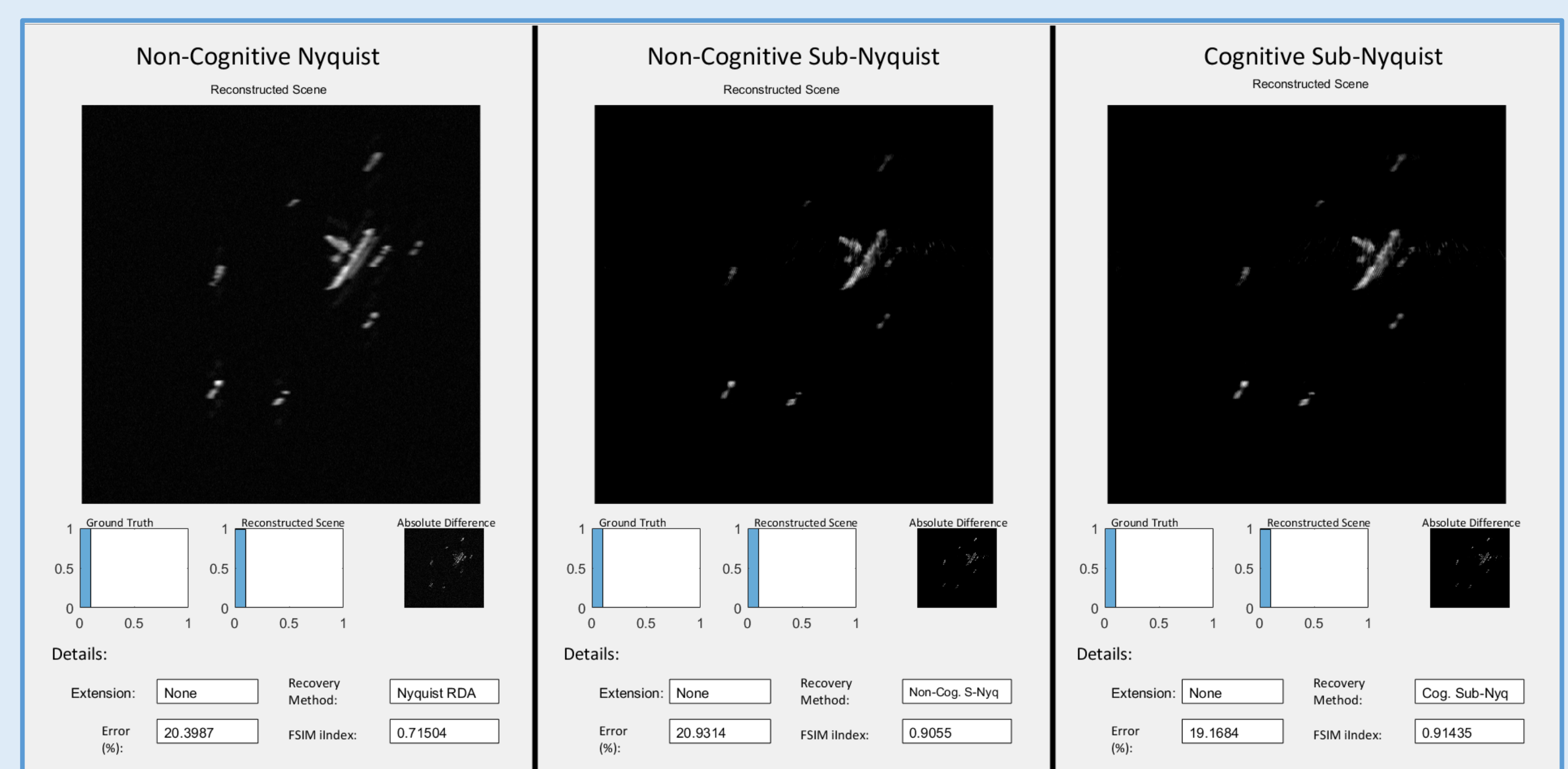
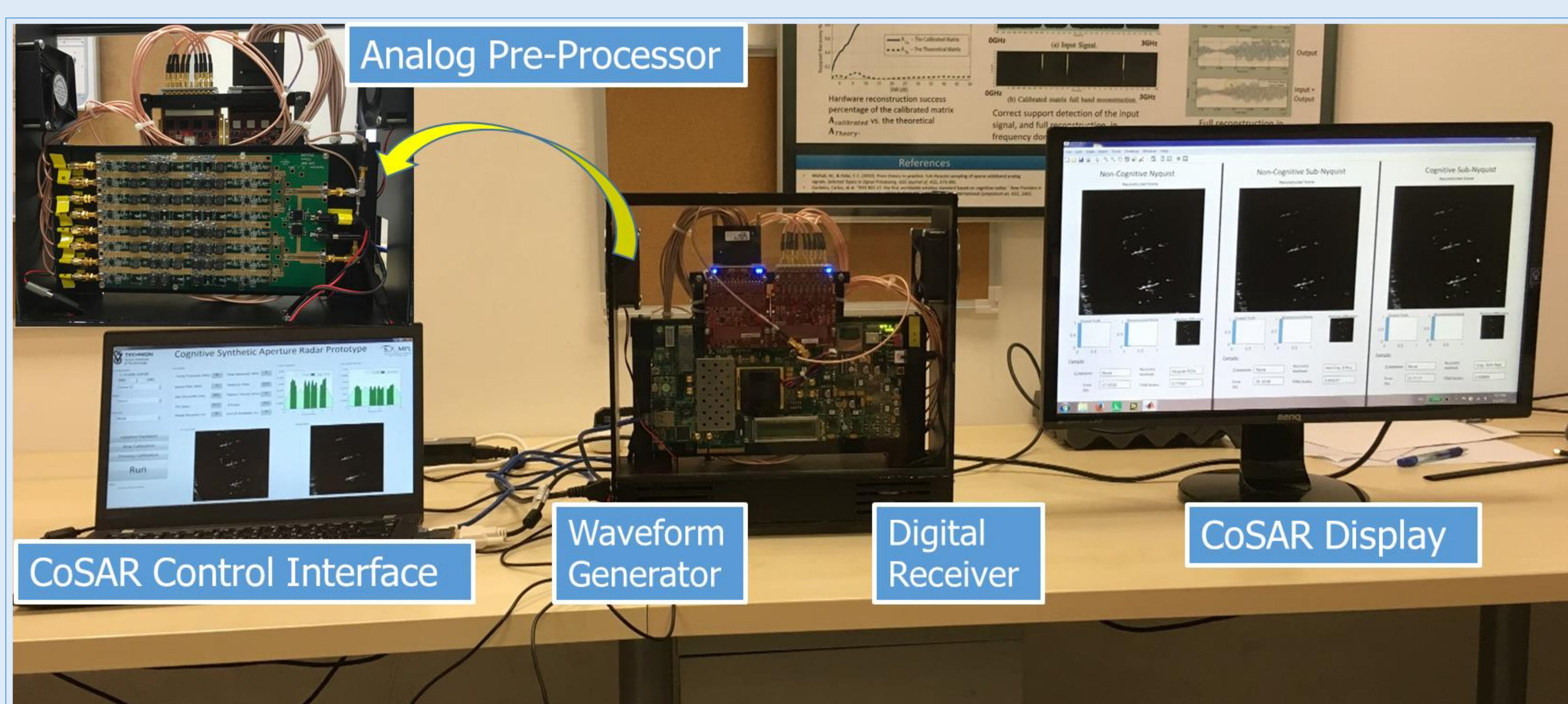


Waveform Generator and Digital Receiver



- Single Xilinx Virtex VC707 Board
- 4DSP DAC and ADC daughter boards for generator and receiver
- Separate streams for I and Q signals

CoSAR Prototype and Measurement Results



CoSAR recovers the target scene sampled at 1/4th and processed at 1/8th of the Nyquist rate with least error and most similar low-level features